# Security Evaluation of the SPECTR-128 

# Block Cipher 

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#### Abstract

The evaluation of availability in resistant to differential and linear cryptanalytic attacks is essential in designing secure block ciphers. In this paper, we present evaluated results of security estimation for SPECTR-128 block cipher. The results show that SPECTR'-128 (modified version of SPECTR-128) is a highly-resistant to differential and linear cryptanalytic attacks.


Keywords: Controlled permutations (CP), data-dependent permutations (DDP), internal key scheduling (IKS), differential cryptanalysis (DC), linear cryptanalysis (LC).

## 1 Introduction

SPECTR-128 is a block cipher proposed by Moldovyan N.A in [1]. The specification of SPECTR-128 can be found in [1]. An overview of its architecture is given in Fig. 1.
This cipher is based on extensive use of CP-box operations. The left data subblock is used to specify the permutations on the right data subblock and roundsubkey. The use of two mutually inverse DDP performed sequentially on the right subblock allows one to perform enciphering and deciphering with the same algorithm. A single-layer CP-box is used to quickly change the key schedule while changing encryption mode for decryption one. A peculiarity of SPECTR-128 is the use of the data-dependent transformation of round subkeys (so called internal key scheduling [2] - IKE). It is based on a combination of DDP and special fast operation $G[3,4]$ in order to greatly reduce the effectiveness of differential and linear cryptanalysis.

This paper provides the results of a cryptographic evaluation of SPECTR-128 (SPECTR'-128).
This paper is organized as follows. In Section 2, we briefly present 128 -bit cipher SPECTR-128. Sections 3 and 4 present differential and linear cryptanalytic attacks of SPECTR-128, respectively. Finally, we conclude in Section 5.

## 2 Description of SPECTR-128

SPECTR-128 is a new 12-round block cipher with 128-bit input. The general encryption scheme is defined by the following formulas: $C=\operatorname{Encr}(M, K)$ and $M=\operatorname{Decr}(C, K)$, where $M$ is the plaintext, $C$ is the cipher text $\left(M, C \in\{0,1\}^{128}\right), K$ is the secret key ( $K \in\{0,1\}^{256}$ ), Encr is the encryption function, and Decr is the decryption function. In the block cipher SPECTR-128 encryption and decryption functions are described by formula $Y=\mathbf{F}\left(X, Q^{(e)}\right)$, where $Q^{(e)}=\mathbf{H}(K, e)$ is the extended key (EK), the last being a function of the secret key $K=\left(K_{1}, \ldots, K_{4}\right)$ and of the transformation mode parameter $e$ ( $e=0$ defines encryption, $e=1$ defines decryption). We have $X=M$, for $e=0$ and $X=C$ for $e=1$. EK is represented as concatenation of 14 subkeys: $Q^{(e)}=\left(Q_{I T}^{(e)}, Q_{1}^{(e)}, \ldots, Q_{12}^{(e)}, Q_{F T}^{(e)}\right)$ where $Q_{I T}^{(e)}, Q_{F T}^{(e)} \in\{0,1\}^{64}$ and $\forall j=1, \ldots, 12, Q_{j}^{(e)}=\left(Q_{j}^{(1, e)}, \ldots, Q_{j}^{(4, e)}\right)$, where $\forall h=1, \ldots, 4, Q_{j}^{(h, e)} \in\{0,1\}^{(44}$. Output value $Y$ is the ciphertext $C$ in the encryption mode or the plaintext $M$ in the decryption mode.

The algorithm is designed as sequence of the following procedures [1]: 1) initial transformationIT, 2) 12 rounds with procedure Crypt, and 3) final transformationFT. Ciphering begins with the procedure IT: $Y^{\prime}=\mathbf{I T}\left(X, Q_{I T}^{(e)}\right)$. Then data
block $Y^{\prime}$ is divided into two 64-bit blocks $L_{0}$ and $R_{0}$, i.e. $\left(L_{0}, R_{0}\right)=Y^{\prime}$, where $L_{0}, R_{0} \in\{0,1\}^{64}$. Then twelve sequential rounds are performed with procedures Crypt in accordance with the formulas: $L_{j}=\operatorname{Crypt}\left(R_{j-1}, L_{j-1}, Q_{j}^{(e)}\right) ; R_{j}=L_{j-1}$, where $j=1, \ldots, 12$. Then the final transformation $\mathbf{F T}$ is executed: $Y=\mathbf{F T}\left(X, Q_{F T}^{(e)}\right.$, where $X=\left(R_{12}, L_{12}\right)$. The general encryption scheme is shown in Figure 1.


Figure1. General structure of SPECTR-128

The structure of the procedure Crypt is shown in Figure 2.


Figure2.Structure of the procedure Crypt
This procedure has the form: $R=\mathbf{C r y p t}\left(R, L, A^{(1)}, A^{(2)}, A^{(3)}\right.$ and $\left.A^{(4)}\right)$ where $R$, $L, A^{(1)}, A^{(2)}, A^{(3)}, A^{(4)} \in\{0,1\}^{64}$. Thus, Crypt transforms the data subblock $R$ under
control of the data subblock $L$ and 256-bit extendedsubkey. This procedure uses the following operations: to-left cyclic rotation "<<<" by fixed number of bits, XOR operation " $\oplus$ ", non-linear operation $\mathbf{G}$, DDP operations $\mathbf{P}_{64 / 192}$ and $\mathbf{P}^{-1}{ }_{64 / 192}$, and extension operation $\mathbf{E}$.

For the block cipher SPECTR-128 see more details in [1].

## 3 Differential Cryptanalysis

### 3.1 Some properties of the controlled operations

Let $\Delta_{q}^{w}$ be the difference with arbitrary $q$ active (non-zero) bits corresponding to the vector $W$. Let $\Delta_{q i i_{i, \ldots, i_{s}}}$ be the difference with $q$ active bits and $i_{1}, \ldots, i_{q}$ be the numbers of digits corresponding to active bits. Note that $\Delta_{1}$ corresponds to one of the differences $\Delta_{1 \mid 1}, \Delta_{1 \mid 2}, \ldots, \Delta_{1 \mid 64}$. Let $P\left(\Delta_{q} \xrightarrow{\mathrm{~F}} \Delta_{g}^{\prime}\right)$ be the probability that input difference $\Delta_{q}$ transforms into output difference $\Delta^{\prime}{ }_{g}$ while passing some operation $\mathbf{F}$. We shall also denote the event that at the output or input of the operation $\mathbf{F}$ we have the difference $\Delta_{q}$ as $\Delta_{q}^{\mathrm{F}}$ or $\Delta_{q}^{\mathrm{F}}$ respectively.
Differential properties of the CP boxes with the given structure are defined by properties of the elementary switching element. Using the main properties of the last (see Figure 3) it is easy to find characteristics of the $\mathbf{P}_{64 / 192}$-box. Table 1 presents probabilities of different output differences corresponding to differences $\Delta_{q^{\prime}}^{L}$ and $\Delta_{q}^{R}$ with few active bits ( $q^{\prime}, q \in\{0,1,2\}$ ).


Figure3. Properties of the elementary box $\mathbf{P}_{2 / 1}$

Figure 3 illustrates the case when some difference with one active bit $\Delta_{q}^{L}$ passes the left branch of the crypto scheme. The difference $\Delta_{q}^{L}$ can cause generation or annihilation of $w$ pairs of active bits in the CP box. Let consider the $\mathbf{P}_{64 / 192}$-box in right branch in the case $q=1$. The difference $\Delta_{1}^{L}$ is transformed by the extension box into $\Delta_{3}^{v}$ at the controlling input of $\mathbf{P}_{64 / 192}$, i.e. one active bit in the left subblock influences three switching elements $\mathbf{P}_{2 / 1}$ permuting six different bits of the right data subblock.Depending on value of the permuted bits and input difference $\Delta_{q}^{R}$ of the $\mathbf{P}_{64 / 192}$-box the output differences $\Delta_{g}^{\prime R}$ with different number of active bits can be formed by this CP box.

Table1.Values of probability $P\left(\left(\Delta_{q}^{R} \xrightarrow{P_{\text {atur }}} \Delta_{g}^{\prime R}\right) / \Delta_{q^{\prime}}^{L}\right)$

|  | $\Delta_{0}^{R} \rightarrow \Delta_{0}^{\prime R}$ | $\Delta_{0}^{R} \rightarrow \Delta_{2}^{\prime R}$ | $\Delta_{0}^{R} \rightarrow \Delta_{4}^{\prime R}$ | $\Delta_{0}^{R} \rightarrow \Delta_{6}^{\prime R}$ | $\Delta_{1}^{R} \rightarrow \Delta_{1}^{\prime R}$ |  | $\Delta_{1}^{R} \rightarrow \Delta_{3}^{\prime R}$ | $\Delta_{1}^{R} \rightarrow \Delta_{5}^{\prime R}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\Delta_{0}^{L}$ | 1 | 0 | 0 | 0 | 1 |  | 0 | 0 |
| $\Delta_{1}^{L}$ | $2^{-3}$ | $1.5 \cdot 2^{-2}$ | $1.5 \cdot 2^{-2}$ | $2^{-3}$ | $1.1 \cdot 2^{-3}$ |  | $1.55 \cdot 2^{-}$ | $1.45 \cdot 2^{-}$ |
| $\Delta_{2}^{L}$ | $2^{-6}$ | $1.5 \cdot 2^{-4}$ | $1.88 \cdot 2^{-}$ | $1.25 \cdot 2^{-}$ | $\underset{6}{1.19 .2-}$ |  | $1.69 \cdot 2^{-}$ | $2^{-2}$ |
|  | $\Delta_{1}^{R} \rightarrow \Delta_{7}^{\prime R}$ | $\Delta_{2}^{R} \rightarrow \Delta_{0}^{\prime R}$ | $\Delta_{2}^{R} \rightarrow \Delta_{2}^{\prime R}$ | $\Delta_{2}^{R} \rightarrow \Delta_{4}^{\prime R}$ |  | $\Delta_{2}^{R} \rightarrow \Delta_{6}^{\prime R}$ |  | $\Delta_{2}^{R} \rightarrow \Delta_{8}^{\prime R}$ |
| $\Delta_{0}^{L}$ | 0 | 0 | 1 | 0 |  | 0 |  | 0 |
| $\Delta_{1}^{L}$ | $0.91 \cdot 2^{-3}$ | $1.52 \cdot 2^{-13}$ | $1.11 \cdot 2^{-3}$ | $1.42 \cdot 2^{-2}$ |  | $1.27 \cdot 2^{-2}$ |  | $1.64 \cdot 2^{-4}$ |
| $\Delta_{2}^{L}$ | $1.25 \cdot 2^{-2}$ | $1.52 \cdot 2^{-15}$ | $1.1 \cdot 2^{-6}$ | $1.51 \cdot 2^{-4}$ |  | $1.72 \cdot 2^{-3}$ |  | $1.05 \cdot 2^{-2}$ |

Avalanche effect corresponding to the operations $\mathbf{G}$ is defined by its structure that provides each input bit influences several ( $u$ ) output bits (except the 64th input bit influences only the 64th output bit). Table 2 presents the formulas describing avalanche caused by inverting the bit $l_{i}$. Let $\Delta l_{i}$ denote alteration of $l_{i}$. We shall consider the case when the data and key are uniformly distributed random values. One can see that $l_{\text {}}$, where $7 \leq i \leq 55$, causes deterministic alteration of the output bit $y_{i}$ and probabilistic alteration of the output bits $y_{i+1}, y_{i+3}, y_{i+6}, \ldots, y_{i+9}$ which change with probability $p=0.5$ (for $1 \leq i \leq 6$ we have deterministic alteration of $y_{i}$ and $y_{i+3}$, since $\Delta y_{i+3}=\Delta l_{i} l_{-6}$ ). When passing through the operation $\mathbf{G}$ the difference $\Delta_{1 i}^{L}$ can be transformed with certain probability to the output differences $\Delta_{1 \mid}^{Y}, \Delta_{2}^{Y}$, ..., $\Delta_{7}^{Y}$ (see Tables 3 and 4).


Figure 4.Some properties of the CP box: a - notation of the general case; b-zero difference passes the CP box; c - formation of two active bits; d - annihilation of two active bits.

Table 2.Changing output bits caused by single bit alteration ( $\Delta l_{i}=1$ ) at input of the operation G

| $\#$ | Expression | Probability |
| :---: | :---: | :---: |
| 1 | $\Delta y_{i}=\Delta l_{i}$ | $p\left(\Delta y_{i}=1\right)=1$ |
| 2 | $\Delta y_{i+1}=\Delta l_{i}\left(a_{i-1}^{(4)} \oplus a_{i-1}^{(3)} l_{i-8} \oplus a_{i}^{(4)} l_{i-5} l_{i-8)}\right.$ | $p\left(\Delta y_{i+1}=1\right)=1 / 2$ |
| 3 | $\Delta y_{i+2}=0$ | $p\left(\Delta y_{i+2}=1\right)=0$ |
| 4 | $\Delta y_{i+3}=\Delta l_{i-6}$ | $p\left(\Delta y_{i+3}=1\right)=1 / 2$ |
| 5 | $\Delta y_{i+4}=0$ | $p\left(\Delta y_{i+4}=1\right)=0$ |
| 6 | $\Delta y_{i+5}=0$ | $p\left(\Delta y_{i+5}=1\right)=0$ |
| 7 | $\Delta y_{i+6}=\Delta l_{i}\left(l_{i-2} \oplus l_{i-3} l_{i+5} a_{i+5}^{(4)}\right)$ | $p\left(\Delta y_{i+6}=1\right)=1 / 2$ |
| 8 | $\Delta y_{i+7}=\Delta l_{i}^{(3)}$ | $p\left(\Delta y_{i+5}=1\right)=1 / 2$ |
| 9 | $\Delta y_{i+8}=\Delta l_{i} l_{i+2}$ | $p\left(\Delta y_{i+8}=1\right)=1 / 2$ |
| 10 | $\Delta y_{i+9}=\Delta l_{i}\left(l_{i+6} \oplus l_{i+8} a_{i+7}^{(3)} \oplus l_{i+3} l_{i+8} a_{i+8}^{(4)}\right.$ | $p\left(\Delta y_{i+9}=1\right)=1 / 2$ |

Table3.Values of the probability $P\left(\Delta_{\| i l}^{L} \xrightarrow{\mathrm{G}} \Delta_{g}^{\gamma}\right)$

| i | $\Delta_{1 i}^{L} \rightarrow \Delta_{1 i}^{y}$ | $\ldots{ }^{\text {.. } \Delta_{2}^{r}}$ | $\ldots$ | $\ldots{ }^{\text {.. }} \Delta_{4}^{Y}$ | $\ldots{ }^{\prime} . . \Delta_{5}^{Y}$ | $\ldots{ }^{\prime} .$. | $\ldots{ }^{\text {. }}{ }^{\gamma}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1-6 | - | $2^{-5}$ | $1.25 \cdot 2^{-3}$ | $1.25 \cdot 2^{-}$ | $1.25 \cdot 2^{-2}$ | $1.25 \cdot 2^{-}$ | $2^{-5}$ |
| 7-55 | $2^{-5}$ | $1.5 \cdot 2^{-4}$ | ${ }_{3}^{1.875 \cdot 2}$ | $1.25 \cdot 2^{-}$ | $1.875 \cdot 2^{-}$ | $1.5 \cdot 2^{-4}$ | $2^{-6}$ |
| 56 | $2^{-5}$ | $1.25 \cdot 2^{-}$ | $1.25 \cdot 2^{-2}$ | $1.25 \cdot 2^{-}$ | $1.25 \cdot 2^{-3}$ | $2^{-5}$ | - |
| 57 | $2^{-4}$ | $2^{-2}$ | $1.5 \cdot 2^{-2}$ | $2^{-2}$ | $2^{-4}$ | - | - |
| 58 | $2^{-3}$ | $1.5 \cdot 2^{-2}$ | $1.5 \cdot 2^{-2}$ | $2^{-3}$ | - | - | - |
| $\begin{gathered} \hline 59- \\ 61 \end{gathered}$ | $2^{-2}$ | $2^{-1}$ | $2^{-2}$ | - | - | - | - |
| 62,63 | $2^{-1}$ | $2^{-1}$ | - | - | - | - | - |
| 64 | 1 | - | - | - | - | - | - |

Table 4.Values of the probability $P\left(\Delta_{\| i i}^{L} \xrightarrow{G} \Delta_{2 \mid, i, i}^{\gamma}\right)$

| $i$ | $u$ | $\Delta_{1 i j}^{L} \rightarrow \Delta_{2 l i, i+1}^{Y}$ | $\ldots{ }^{. .} \Delta_{2 l, i+3}^{Y}$ | $\ldots . . \Delta_{2 i, 1+6}^{Y}$ | $\ldots{ }^{\text {. }} \Delta_{2 l i, i 7}^{Y}$ | $\ldots{ }^{\text {. }} \Delta_{21, i+8}^{Y}$ | $\ldots$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1-6 | 7 | - | $2^{-5}$ | - | - | - | - |
| $\begin{array}{r} 7- \\ 55 \\ \hline \end{array}$ | 7 | $2^{-6}$ | $2^{-6}$ | $2^{-6}$ | $2^{-6}$ | $2^{-6}$ | $2^{-6}$ |
| 56 | 6 | $2^{-5}$ | $2^{-5}$ | $2^{-5}$ | $2^{-5}$ | $2^{-5}$ | - |
| 57 | 5 | $2^{-4}$ | $2^{-4}$ | $2^{-4}$ | $2^{-4}$ | - | - |
| 58 | 4 | $2^{-3}$ | $2^{-3}$ | $2^{-3}$ | - | - | - |
| $\begin{aligned} & \hline 59- \\ & 61 \\ & \hline \end{aligned}$ | 3 | $2^{-2}$ | $2^{-2}$ | - | - | - | - |
| $\begin{aligned} & \hline 62- \\ & 63 \end{aligned}$ | 2 | $2^{-1}$ | - | - | - | - | - |
| 64 | 1 | - | - | - | - | - | - |

### 3.2 Differential analysis

Our best variant of the differential cryptanalysis (DCA) [5, 6] of SPECTR-128 corresponds to two-round characteristic with difference $\left(\Delta_{0}^{L}, \Delta_{1}^{R}\right)$. This difference passes two rounds in the following way (see Figure 5). It is easy to see that this difference passes the first round with probability 1 and after swapping subblocks it transforms to $\left(\Delta_{1}^{L}, \Delta_{0}^{R}\right)$. In the second round the active bit passing through the left branch of crypto scheme can form at the output of the operation $\mathbf{G}$ the difference $\Delta_{g}^{Y}$, where $g \in\{1,2,3,4,5,6,7\}$. Only differences with even number of active bits contribute to the probability of the two round iterative characteristic. The most
contributing are the differences $\Delta_{2 i, i+k}^{Y}$. The most contributing mechanisms of the formation of the two-round characteristic belong to Cases 1,2 , and 3 , where $i \in\{1, \ldots, 64\}$ and $k \in\{1,3,6,7,8,9\}$, described below.

## Case 1:

- Difference $\Delta_{2 l i, i+k}^{V}$ is formed with probability $p_{2}^{(i, i+k)}=\operatorname{Pr}\left(\Delta_{2 l i, i+k}^{\mathrm{G}} / \Delta_{l i f}^{\mathrm{G}_{\mathrm{V}}}\right)$ at the output of the operation $\mathbf{G}$.
- Difference $\Delta_{2 l i, i+k}^{\prime}$ is formed with probability $p_{3}^{(i, i+k)}=\operatorname{Pr}\left(\Delta_{2 l i, i+k}^{p_{i}^{\prime}} / \Delta_{0}^{P_{i}^{\prime}}\right)$ at the output of the CP box $\mathbf{P}^{\prime}$.
- Difference $\Delta^{\prime \prime}{ }_{0}$ is formed with probability $p_{1}=2^{-3}=\operatorname{Pr}\left(\Delta_{0}^{p^{\dot{p}}} / \Delta_{0}^{\left.p^{\dot{p}}\right)}\right.$ ) at the output of the CP box $\mathbf{P}$ ".
- After XORing differences $\Delta_{2 l, i+k}^{V}, \Delta^{\prime}{ }_{2 l i, i+k}$, and $\Delta^{\prime \prime}{ }_{0}$ we have zero difference $\Delta_{0}$ at the input of the $\mathbf{P}^{*}$-box. It passes this box with probability $p_{4}=2^{-3}=\operatorname{Pr}\left(\Delta_{0}^{\mathrm{P}^{\dot{p}}} / \Delta_{0}^{\mathrm{P}^{\mathrm{P}}}\right)$.
One can denote Case 1 as set of the following events:

Using such form of representation one can describe the following two cases:


Values $p_{1}^{(i, i+k)}, p_{3}^{(i, i+k)}$, and $p_{4}^{(i, i+k)}$ are calculated in the similar way using the structure of the box $\mathbf{P}_{64 / 192}$ and distribution of the controlling bits over elementary switching boxes $\mathbf{P}_{2 / 1}$ (this distribution is defined by Table A-2 and operation ">>>21"). For example, let us consider the mostly contributing difference $\Delta_{143}^{L}$ while calculating $p_{3}^{(i, i+k)}$. After being rotated by 21 bits this difference induces the difference $\Delta_{3}^{v}=\Delta_{3109,13,1,122}^{v}$ at the 192-bit controlling input of the CP box $\mathbf{P}_{64 / 192}$ transforming the right data subblock $R$. The 43d bit of $L$ controls one elementary box $\mathbf{P}_{2 / 1}$ in each of three lower active layers of the CP box $\mathbf{P}_{64 / 192}$, namely the 109th, 133d, and 182nd boxes $\mathbf{P}_{2 / 1}$ (such elementary boxes can be called active). For $i=43$ we have six variants of $\Delta_{2 l i, j}^{Y}: \Delta_{243,44}^{Y}, \Delta_{243,46}^{Y}, \Delta_{2443,49}^{Y}, \Delta_{243,50}^{Y}, \Delta_{243,51}^{Y}$, and $\Delta_{243,52 .}^{Y}$. For the corresponding probabilities $p_{3}^{(i, j)}$ we have zero value, except $p_{3}^{(4,34)}=2^{-3}$. The last value takes into account that the 109th and 133d boxes $\mathbf{P}_{2 / 1}$ do not generate non-zero output difference and the 182nd one generates two active bits.


Figure 5.Formation of the two-round differential characteristic in Case 1
Taking into account the symmetric structure of the round transformation and symmetry of the boxes $\mathbf{P}_{64 / 192}$ and $\mathbf{P}^{-1}{ }_{64 / 192}$ it is easy to see that $P^{\prime \prime \prime}=P^{\prime}$, where $P^{\prime}$ and $P^{\prime \prime \prime}$ are the contributions to the probability of the two-round differential characteristic corresponding to the first and third cases. Thus, it is sufficient to calculate $P^{\prime}$ and the contribution $P^{\prime \prime}$ of the second case. Due to different rotations before extension boxes corresponding to CP-box operations $\mathbf{P}^{\prime}$ and $\mathbf{P}^{\prime \prime}$ we have $P^{\prime \prime \prime} \neq P^{\prime}$.

Probability $P^{\prime}$ can be calculated using the following formula:
$P^{\prime}=p(i) \sum_{i, k} p_{1} p_{2}^{(i, i+k)} p_{3}^{(i, i+k)} p_{4}=2^{-12} \sum_{i, k} p_{2}^{(i, i+k)} p_{3}^{(i, i+k)} \approx 1.5 \cdot 2^{-21}$, where $p(i)=2^{-6}$ corresponds to probability that after the first round active bit moves to the $i$ th digit. The value $P^{\prime}$ is defined mainly by the digit $i=43$ (about $70 \%$ ) for which we have $p_{3}^{(4,34)}=2^{-3}$. About $15 \%$ corresponds to digits $i=33$ and $i=34$ and about $15 \%$ correspond to digits $i=3,7,8,11,12,15,16,20,54$. For all other digits we have zero contribution to $P^{\prime}$.

Probability $P^{\prime \prime}$ can be calculated analogously to the case of $P^{\prime}$ : $P^{\prime \prime}=p(i) \sum_{i, k} p_{1}^{(i, i+k)} p_{2}^{(i, i+k)} p_{3} p_{4} \approx 1.5 \cdot 2^{-21}$. The digits contributing to $P^{\prime \prime}$ are only the following: $i=54,57\left(p_{1}^{(54,5)}=p_{1}^{(5,50)}=2^{-5}\right)$, and $i=9,10,11,44$
$\left(p_{1}^{(9,15)}=p_{1}^{(9,16)}=p_{1}^{(10,13)}=p_{1}^{(0,16)}=p_{1}^{(11,4)}=p_{1}^{(4,4,4)}=p_{1}^{(4,4,4)}=2^{-7}\right)$. Due to symmetry of the boxes $\mathbf{P}^{\prime}$ and $\mathbf{P}^{*}$ there are possible contributing events (analogous to Cases 1-3) including generation of the additional pair of active bits in $\mathbf{P}^{\prime}$ and annihilation of these bits in $\mathbf{P}^{*}$. The contribution of such events is $P_{0} \approx 1 \cdot 1 \cdot 2^{-21}$. For probability of the two-round characteristic we have $\mathrm{P}(2) \approx P^{\prime}+P^{\prime \prime}+P^{\prime \prime \prime}+P_{0} \approx 1.4 .2^{-19}$.

### 3.3 Modified version SPECTR’-128

Differential analysis has shown that the structure of the extension box (i.e. the table describing distribution of the bits of the left data subblock over elementary switching elements of the CP boxes) is a critical part of SPECTR-128. It is easy to see that small change in the extension box leads to significant decrease or increase of the probability of two-round characteristic. Indeed, we can reduce the probability $\mathrm{P}(2)$ by factor $\approx 2^{8}$ using the extension box described by the Table 5 .

Table 5.Distribution of bits of the vector $U$

| $V_{1}$ | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 62 | 63 | 34 | 60 | 35 | 36 | 37 | 43 | 44 | 54 | 55 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | $V_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $V_{2}$ | 50 | 41 | 52 | 53 | 42 | 61 | 56 | 57 | 61 | 38 | 48 | 55 | 45 | 46 | 47 | 49 | 64 | 49 | 50 | 51 | 38 | 39 | 40 | 41 | 42 | 48 | 53 | 45 | 46 | 47 | 52 | 33 | $V_{2}$ |
| $V_{3}$ | 58 | 59 | 45 | 58 | 62 | 49 | 64 | 63 | 33 | 51 | 52 | 53 | 54 | 55 | 39 | 54 | 57 | 46 | 44 | 60 | 43 | 47 | 48 | 50 | 34 | 35 | 36 | 37 | 59 | 56 | 40 | 51 | $V_{3}$ |
| $V_{4}$ | 26 | 27 | 28 | 29 | 1 | 19 | 10 | 17 | 18 | 31 | 20 | 21 | 14 | 23 | 24 | 25 | 32 | 11 | 8 | 9 | 22 | 15 | 16 | 30 | 2 | 3 | 4 | 5 | 6 | 7 | 12 | 13 | $V_{4}$ |
| $V_{5}$ | 18 | 19 | 20 | 21 | 14 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 17 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 1 | 12 | 13 | 22 | 15 | 16 | 11 | $V_{5}$ |
| $V_{6}$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 28 | 23 | 24 | 25 | 26 | 27 | 22 | 29 | 30 | 31 | 32 | $V_{6}$ |

Let call the modified version SPECTR'-128. For SPECTR'-128 cases 1, 2, and 3 give zero contribution to the probability of two-round characteristic. After modification of $\mathbf{E}$-box the most contributing cases are the following ( $\forall i, t, k i, t \in\{1,2, \ldots, 64\}, k \in\{1,3,6,7,8,9\}, t \neq i$, and $t \neq i+k$ ).

Calculating the total contribution of the cases $4 \mathrm{a}, 4 \mathrm{~b}, 5 \mathrm{a}, 5 \mathrm{~b}, 6 \mathrm{a}$, and 6 b we have obtained $P(2)=1.85 \cdot 2^{-28} \approx 2^{-27}$. Thus, after modification of the extension box the value $P(2)$ has been significantly reduced. Now the three-round characteristic becomes the most efficient one. One of possible mechanisms of the formation of this characteristic is shown in Fig. 5. This characteristic does not depend on small modifications of the distribution table. In the most contributing mechanisms of the formation of the three-round characteristic in second and third rounds the operation $\mathbf{G}$ produces output difference exactly with one active bit.

To calculate probability $p_{2}=p\left(\Delta_{1 i}^{\mathrm{G}} / \Delta_{1 i i}^{\mathbf{G}_{\mathrm{i}}}\right)$ one should take into account its dependence on $i$. Let $p_{2}^{(i)}$ be the probability that the output difference of $\mathbf{G}$ has exactly one active bit corresponding to theith digit. Probability $p_{2}^{(i)}$ is equal to $2^{-6}$ for $i \in\{7, \ldots, 55\}, 2^{-5}$ for $i=56,2^{-4}$ for $i=56,2^{-3}$ for $i=58,2^{-2}$ for $i \in\{59,60,61\}, 2^{-1}$ for $i \in\{62,63\}, 1$ for $i=64$, and 0 for $i \in\{1, \ldots, 6\}$. For uniformly distributed random value $i$ we have the average value $p_{2} \approx 0.93 \cdot 2^{-4}$ while considering the operation $\mathbf{G}$ as individual unit. Probability that in the second round the $\mathbf{P}^{\prime \prime}$-box generates no pairs of active bits is $p^{(i)}=2^{-3}$ for all $i$. The same probability corresponds to the individual boxes $\mathbf{P}^{\prime}$ and $\mathbf{P}^{*}$, however, because of their mutual symmetry one has to consider these two boxes as a single unit. Probability that they generate no pair of active bits at the output of the operation $\mathbf{P}^{*}$ is $p_{3,4}^{(i)} \approx 2^{-6}$ for $i \in\{1,2, \ldots, 21,54, \ldots, 64\}$ and $p_{3,4}^{(i)} \approx 1.32 \cdot 2^{-5}$ for $i \in\{22,23, \ldots, 53\}$. The last value takes into account the cases of including generation, and annihilation of the pairs of active bits in the boxes $\mathbf{P}^{\prime}$ and $\mathbf{P}^{*}$. If at the input of the first round we have the difference $\left(\Delta_{0}^{L}, \Delta_{1}^{R}\right)$, then at the output of the second round we have the difference $\left(\Delta_{1}^{L}, \Delta_{1}^{R}\right)$ with probability $p^{\prime}=2^{-6} \sum_{i} p_{1}^{(i)} p_{2}^{(i)} p_{3,4}^{(i)} \approx 1.14 \cdot 2^{-13} \cdot \frac{n!}{r!(n-r)!}$

In the third round the active bit passing the box $\mathbf{P}^{\prime}$ is XORed with the single output active bit of the operation $\mathbf{G}$ with probability $p^{\prime \prime}=2^{-6}$ and no new active bits are formed by operations $\mathbf{G}, \mathbf{P}^{\prime}, \mathbf{P}$ ", and $\mathbf{P}^{*}$ with probability $p^{\prime} \approx 1.14 \cdot 2^{-13}$. Thus, for probability of the three-round characteristic we get $P(3)=p^{\prime 2} p^{\prime \prime} \approx 1 \cdot 3 \cdot 2^{-32}$.

Contribution of the two-round characteristic to the value $P(12)$ is $P_{(2)}(12)=$ $P^{6}(2) \approx\left(2^{-27}\right)^{6}=2^{-162}$. Contribution of the three-round characteristic is $P_{(3)}(12)=P^{4}(3) \approx 1 \cdot 4 \cdot 2^{-127} \gg P_{(2)}(12)$. Probability to have at output of the random cipher the difference $\left(\Delta_{0}^{L}, \Delta_{1}^{R}\right)$ is equal to $2^{-122} \gg P_{(3)}(12)$. Thus, the cipher SPECTR'128 with twelve encryption rounds is undistinguishable from a random cipher with the most efficient differential characteristic.


Figure 6.Formation of the three-round differential characteristic (mechanisms including generation of the active bits in the CP boxes are not shown)

## 4 Linear Cryptanalysis

Comparison of the known results on security estimation of the DDP-based ciphers shows that linear cryptanalysis (LCA) [7, 8] appears to be less efficient to attack DDP-based ciphers as compared with DCA. For example, to thwart the linear attack against SPECTR-H64 (DDP-64) seven [9] (three [10]) rounds are sufficient whereas to thwart the differential attack on that cipher at least ten [11] (eight [10]) rounds are required. Fixed permutations and the DDP operations are bijections that preserve the Hamming weight of the input vector, however to use this property in a linear attack one should apply masks having maximum weight. Such
masks are note efficient due to non-linear operations used together with DDP. Detailed theory of the linear characteristics (LC) of the CP-boxes is presented in [9]. Let denote an input mask as $M$ and the output mask as $B$. In that paper it has been shown that:
i) Bias of arbitrary LC for which $\varphi(M) \neq \varphi(B)$ is equal to zero;
ii) For the CP-boxes of the order $h \geq 1$ for $\varphi(M)=\varphi(B) \geq 1$ the bias $b$ of the DDP operation satisfies condition $b \leq \frac{1}{2 n}$ independently of the mask assigned to the controlling input of the CP-box (for the boxes $\mathbf{P}_{64 / 192}$ we have $b \leq 2^{-7}$ ); the value $b=\frac{1}{2 n}$ corresponds to the to the masks with weight 1 .
iii) Linear attacks using masks $(1,1, \ldots, 1)$ are prevented efficiently with the G-like operations.
Performing linear analysis of the round transformation of SPECTR-128 we have found that the most efficient LC corresponds to the masks with two active bits in the left utmost positions in each of two data subblock s. Such mask works well in the case of key in whichsubkeys $K_{1}$ and $K_{2}$ as well as $K_{3}$ and $K_{4}$ contain equal bits in positions number $18,25,29,50,57$. Probability to select such key is $2^{-10}$. Let denote the mask corresponding to vector $X$ as $M_{q i, \ldots, i, i}^{x}$, where $q$ is the number of active bits and $i_{1}, \ldots, i_{q}$ are the indices of the active bits. The LC with input ( $M_{\mu 11}^{L_{0}}, M_{11}^{R_{0}}$ ) and output ( $M_{41}^{L_{1}}, M_{11}^{R_{1}}$ ) masks of the first round has bias $b(1) \leq 2^{-7}$. The last value is calculated as follows (see fig.7). Note that for considered particular case of keys the $\mathbf{P}^{*}$-box moves the left most input bit to the left most digit at the output, if the $\mathbf{P}^{\prime}$-box moves the left most input bit to the left mostdigit at its output. Bias of the considered one-round LC is

$$
b(1)=\left|\operatorname{Pr}\left(L_{0} \bullet M_{1 \mid i}^{L_{0}} \oplus R_{0} \bullet M_{1 \mid i}^{R_{0}} \oplus L_{1} \bullet M_{1| |}^{L_{1}} \oplus R_{1} \bullet M_{1 \mid 1}^{R_{1}}=1\right)-\frac{1}{2}\right| .
$$

If the $\mathbf{P}$ '-box moves the left umost input bit to the left umost digit at its output we have

$$
\sigma=L_{0} \bullet M_{1 \mid 1}^{L_{0}} \oplus R_{0} \bullet M_{1 \mid 1}^{R_{0}} \oplus L_{1} \bullet M_{1 \mid 1}^{L_{1}} \oplus R_{1} \bullet M_{1 \mid 1}^{R_{1}}=l_{01} \oplus a_{1}^{(3)} \oplus 1 \oplus z_{1},
$$

where $_{1}$ is the first bit of the vector Z at the output of the CP box $\mathbf{P}$ '. Probability of this event is $1 / n=2^{-6}$. Probability that $\sigma=l_{01} \oplus a_{1}^{(3)} \oplus 1$ is $t / n^{2}$, where $t=\varphi\left(A^{(3)}\right)$. If the $\mathbf{P}$ '-box moves any other input bit to the left umost digit at its output then we have $\sigma=l_{01} \oplus a_{1}^{(3)} \oplus 1$ with probability $2^{-1}(1-1 / n)$ independently of the value $z_{1}$. Thus, we have $\operatorname{Pr}\left(\sigma=l_{01} \oplus a_{1}^{(3)} \oplus 1\right)=\frac{1}{2}-\frac{1}{2 n}+\frac{t}{n^{2}}$ and

$$
b(1)=\left|\operatorname{Pr}(\sigma=1)-\frac{1}{2}\right|=\left|\operatorname{Pr}(\sigma=0)-\frac{1}{2}\right|=\left|-\frac{1}{2 n}+\frac{t}{n^{2}}\right| \leq \frac{1}{2 n} .
$$



Figure7.Formation of the one-round linear

The bias gets maximum value for the cases $\varphi\left(A^{(3)}\right)=1$ and $\varphi\left(A^{(3)}\right)=0$. For the full round SPECTR-128 the LC with input $\left(M_{11}^{L_{0}}, M_{11}^{R_{11}}\right)$ and output $\left(M_{11}^{L_{n}}, M_{111}^{R_{n}}\right)$ masks have bias

$$
b(12)=\frac{1}{2}(2 b(1))^{12} \leq \frac{1}{2 n^{12}}=2^{-73} . \infty
$$

For eleven rounds we have $b(11) \leq 2^{-67}$. For the random cipher LCs have bias $b \approx 2^{-64}>b(11)$. Therefore we can conclude that for the worst case of the secret key selection eleven rounds of SPECTR-128 are sufficient to thwart linear attacks. In order to eliminate linear attacks based on the considered LC we propose to use in the modified version SPECTR'-128 the constant C = (101010...10) instead of thesubkey $A^{(3)}$ (earliersuch mechanism was used in DDP-64 [14]). Since in this case we have $t=\varphi(C)=n / 2$, the bias of the considered characteristic equals to zero, therefore an attacker should add at least one active bit in used masks and this will reduce sharply the bias value due to both the variable permutations and the $\mathbf{G}$ operation.

## 5 Conclusion

Security of the 128-bit block cipher SPECTR-128 is based on the use of DDP performed with $\mathbf{P}_{64 / 192 \text {-boxes, specially designed extension boxes, and the nonlin- }}$ ear operation $\mathbf{G}$.

Some remarks should be given about IKS. Actually it is a part of the round data transformation only. It introduces no delay, since it is executed in parallel with some data ciphering operations. Notion IKS corresponds to the part of encryption procedure related to the data-dependent transformation ofsubkey (orsubkeys) executed in parallel with the transformation of data. The internal key scheduling used in SPECTR-128 is not complex, but it changes from one data block to another, making the avalanche effect faster and crypto scheme significantly more secure against differential and linear cryptanalysis.

In one round of SPECTR-128 the left data subblock is kept constant, however this data subblock participates in round transformation influencing transformation of the right data subblock. Our DCA of SPECTR-128 has shown that the structure of the extension boxes is a critical part of the DDP-based ciphers. Presenting the modified version SPECTR'-128 we have shown the small modifications in the table describing the extension box significantly change the probability of the differential characteristics. Our preliminary LCA shows that SPECTR-128 secure against linear attacks, although much more work on LCA of this cipher is to be done. Because of the use very simple key scheduling there are possible weak keys having the structure $K=\left(K_{1}, K_{2}, K_{3}, K_{4}\right)=(X, X, Y, Y)$, their portion $\left(2^{-128}\right)$ is negligible though. An interesting way to avoid weak keys is the use of the switchable (e-dependent) operations, one can use some complex key scheduling though (weak we call the keys for which encryption function is involution).

The aim of the description and discussion of the SPECTR ciphers is to illustrate the design of the DDP-based ciphers and to show that such ciphers represent a suitable model for calculation of the differential characteristics and security estimations. We estimate that introducing small changes if the structure of the operation $\mathbf{G}$ one can easy reduce the probability of the three-round differential characteristic and design secure ten-round or eight-round SPECTR-like cryptosystem. For example it is easy to compose a $\mathbf{G}$-like function $\mathbf{G}^{\prime}$ for which two output bits change deterministically when an input bit flips. Use of the operation $\mathbf{G}^{\prime}$ in SPECTR reduces drastically the probability of the two-round and three-round differential characteristics as well as the bias of linear characteristics. Detailed design of the SPECTR-like cryptosystem with reduced number of rounds appears to be a subject of separate consideration.

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