

Using Dimension Reduction with Feature Selection to Enhance Accuracy of Tumor Classification

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Abstract—Gene expression microarray data is one of the most popular for diagnosis of cancer. However, the microarray data have thousands of genes and very few samples, it is crucial to develop techniques to effectively gene selection for analysis. So, dimension reduction is an important issue for analysis, of which principle component analysis (PCA) is one of the frequently used methods, and in the previous works, the top several principle components are selected for modeling according to the descending order of eigenvalues. While in this paper, we argue that not all the first features are useful, but features should be selected from all the components by feature selection methods. We demonstrate a framework for selecting good feature subsets from all the principle components, leading to enhance classifier accuracy rates on the gene expression microarray data. As a case study, we have considered PCA for dimension reduction, decision tree algorithms (DT) for feature selection, and then Multi Layer Perceptron network (MLP) for classification. Experimental results illustrate that our proposed framework is effective to enhance classification accuracy rates

Keywords—PCA, DT, MLP, feature selection, microarray, classification.

I. INTRODUCTION

DNA microarray experiments are used to collect information from tissue and cell samples regarding gene expression differences for tumor diagnosis [1-3]. The microarray data have thousands of genes and very few samples, it is crucial to develop techniques to effectively gene selection for analysis. To overcome this problem, we can either select a small subset of interesting genes (gene selection) or construct K new components summarizing the original data as well as possible, with K components \ll Sample. There are some methods of input space dimension reduction such as correlation [4] and variable ranking [5]. Each method puts more emphasis on one aspect than another. In this paper, we propose using PCA for dimension reduction and then using decision tree algorithms to search the space of eigenvectors with the goal of selecting a subset of eigenvectors encoding important information. This approach has the advantage of simple, general, and powerful.

II. METHOD

Our tumor classification system using supervised learning has three main step. The main difference from the traditional approach is that performs feature selection among the principle components extracted by feature extraction. Dimension reduction step consists of two parts, feature extraction and feature selection, here feature extraction is performed by principle components analysis, and feature selection is performed by decision tree algorithms. They are explained in the following subsection.

A. Feature Extraction Using PCA

Principal components analysis (PCA) is a statistical technique for determining the key variables in a multidimensional data set that explain the differences in the observations, and can be used to simplify the analysis and visualization of multidimensional data sets [6].

Consider a data matrix:

$$\mathbf{X} = \{x_{ij}\} \in R^{n \times p} \quad (1)$$

with n – number of rows (i.e. the number of vectors), p – number of columns (i.e. the data dimensions).

PCA is mathematically defined as an orthogonal linear transformation that transform the data to a new coordinate system such that the greatest variance by any projection of the data comes to lie on the first coordinate (called the first principal component), the second greatest variance on the second coordinate, and so on.

The original data change in different intervals, so we need to standardized values in the column of matrix X:

$$\hat{\mathbf{X}} = \{\hat{x}_{ij}\} \quad (2)$$

with

$$\hat{x}_{ij} = \frac{x_{ij} - g_i}{\sqrt{n}} \quad (3)$$

$$g_i = \frac{1}{n} \sum_{j=1}^n x_{ij} \quad (4)$$

where, g_i is the average value of the j^{th} column of X , given by (4).

Then, \hat{X} will be used to calculate the covariance matrix of the data set given as:

$$\mathbf{V} = \hat{\mathbf{X}}^T \cdot \hat{\mathbf{X}} \quad (5)$$

$\mathbf{V} \in R^{p \times p}$ is a matrix of size $p \times p$.

Next, PCA finds the eigenvalues and the eigenvectors and arranged them in descending order. Suppose p eigenvalues of V are $\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_p$ and p eigenvectors are $\mathbf{u}_1, \mathbf{u}_2, \dots, \mathbf{u}_p$. Then the axis of the new space is eigenvector \mathbf{u}_i . If we use only some k first dimensions (where $k \ll p$) then the new matrix created from the eigenvectors is:

$$\mathbf{U} = [\mathbf{u}_1 | \mathbf{u}_2 | \dots | \mathbf{u}_k] \in R^{p \times k} \quad (6)$$

and the new co-ordinates are:

$$\mathbf{F} = \hat{\mathbf{X}} \cdot \mathbf{U} \quad (7)$$

B. Feature Selection Using Decision Tree Algorithm

The decision tree is a classical model for data recognition and classification [7, 8]. Among different model of decision trees, we will apply in this paper the linear model of binary tree. It means the tree will use only simple single conditions such as “if $x_i \text{ op } A$ ” at its nodes, where the *op* includes comparing operators such as =, >, <, >=, <=.

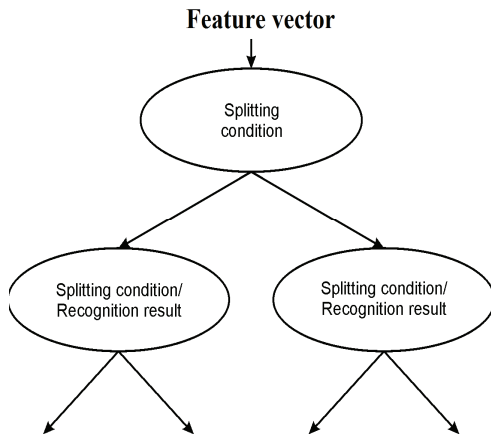


Fig. 1. An Example of Binary Decision Tree

General structure of the decision tree is given in Fig. 1. There are a number of algorithms to train a tree for a given set

of data samples. However, the algorithms to train a tree for a given set of data samples in this paper is ID3 [7, 8], which use the node entropy gain function to optimize the structure of the tree and the splitting conditions for each node of the tree. According to that, if at a node V we have N samples x_1, x_2, \dots, x_N belonging to M classes C_1, C_2, \dots, C_M then the entropy of the node is given as:

$$E(V) = \sum_{i=1}^M -p_i \log_2(p_i) \quad (8)$$

where, $p_i = \frac{|\{x_j : x_j \in C_i\}|}{N}$ is the probability that a sample x_j of

the node belongs to the class C_i . Now with a splitting condition S , the samples from node V are classified to subnodes SV_i (for binary tree $i=1$ or 2) with the appropriate numbers of samples are N_i ($\sum_i N_i = N$). At that time, the entropy gain for node V with splitting condition S is given as:

$$\text{Gain}(V, S) = E(V) - \sum_i \frac{N_i}{N} E(SV_i) \quad (9)$$

A good splitting condition is the one with maximum value of entropy gain for a given node.

C. Multi Layer Perceptron network

MLP is a network of simple neurons called perceptrons [9, 10]. The basic concept of a single perceptron was introduced by Rosenblatt in 1958. The perceptron computes a single output from multiple real-valued inputs by forming a linear combination according to its input weights p and then possibly putting the output $\{\mathbf{x}_i, \mathbf{d}_i\}$ with $i = 1, \dots, p$, $\mathbf{x}_i \in R^N$; $\mathbf{d}_i \in R^K$ through some nonlinear activation function. Mathematically this can be written as:

$$Y = \Psi\left(\sum_{i=1}^n \mathbf{w}_i x_i + b\right) = \Psi(\mathbf{w}^T \mathbf{x} + b) \quad (10)$$

III. EXPERIMENTS

A. Data sets

In the paper, three real data sets obtained from different data sources. Due to the fact, the genetic data from microarray experiments have fewer sample numbers, while some variables (genes) more so to increase the reliability of solutions and research our research use the sample data of different diseases. Brief described as below:

- Leukemia data sets [11,12] were divided into two types of samples: acute lymphoblastic leukemia (ALL) and acute myeloid leukemia (AML) with 47 patients with acute lymphoblastic leukemia (ALL) and 25 patients with acute myeloid leukemia (AML). Each of the 72 patients had bone marrow samples obtained at the time of diagnosis. Furthermore, the observations have been assayed with Affymetrix Hgu6800 chips, resulting in 5327 gene expressions (Affymetrix probes).
- Prostate data sets [13,14] were divided into two types of samples: 52 patients with tumor and 50 patients with normal, resulting in 10509 gene expressions.
- Diffuse large B-cell lymphoma (DLBCL) data sets [15, 16] were divided into two types of samples: 58 DLBCL patients and 19 FL (*Follicular lymphoma*) patients were analyzed according to an Institutional Review Board approved protocol, resulting in 5469 gene expressions.

B. Experimental testing and result

To evaluate the performance of the proposed approach, we use the hold out validation procedure. Each data set is merged as a whole set, then we split the whole set into the training set and test set (2/3 for training data and the rest for test). The training data set is split by keeping 2/3 samples for training, the rest for validation. Classification error of MLPs is obtained on test data sets.

In order to demonstrate the importance of feature selection of dimension reduction, we have performed four series experiments here:

- 1) MLP has achieved satisfactory results, and here it is used without any feature reduction on the data sets.
- 2) PCA+MLP, PCA is a feature extraction method, it is used for dimension reduction without feature selection and the classification of SVM is used. The size of top eigenvectors of PCA is obtained by validating the classifier on the validation data set, as is a traditional way.
- 3) PCA+DT+MLP, beyond the baseline method, we proposed to use DT to select an optimum subset of eigenvectors, since we consider not all the top eigenvectors are useful for discrimination but the tail eigenvectors also contain useful information for discrimination.

Table I show the number of features selected by each on three data sets.

TABLE I. NUMBER OF SELECTED FEATURES

Data sets	MLP	PCA+MLP	PCA+DT+MLP
Leukemia	1+300	6 (PCA1+PCA6)	4 (PCA1,PCA2,PCA4,PCA6)
Prostate	1+500	6 (PCA1+PCA6)	4 (PCA8765,PCA6417,PCA3571,PCA897)
DLBCL	1+500	8 (PCA1+PCA8)	4 (PCA1, PCA2, PCA6, PCA10)

From Table I, we can find feature extraction using PCA + MLP and PCA + DT + MLP have less number inputs of three data sets than using only MLP.

The average error rates are shown in Table 2.

TABLE II. RESULTS OF CLASSIFICATION

Data sets	MLP		PCA+MLP		PCA+DT+MLP	
	Learn error	Test error	Learn error	Test error	Learn error	Test error
Leukemia	3	1	1	1	1	0
Prostate	1	1	2	1	0	0
DLBCL	4	1	1	0	0	0

From Table 2, we can find feature selection by PCA and DT do great help in reducing features and get better result on classification.

C. Discussions

The difficulties of building a classifier for gene expression microarray data are dimension reduction. Here we use the PCA+DT+MLP framework to get a simpler, gender and efficiency classifier. Observing the tables shown in Section 3.2, several interesting comments can be made as below:

- 1) The feature subsets selected by the DT approach improve classification performance, all for the different data sets.
- 2) The DT solutions are quite compact: The final feature subsets found by DT are very compact; the significant reduction in the number of eigenvectors speeds up classification substantially.
- 3) We can find DT both reduces the average error rate and the number of features selected.

IV. CONCLUSION

We have investigated a systematic feature reduction framework by combining feature extraction with feature selection. To evaluate the proposed framework, we used three typical data sets. In each case, we used PCA for feature extraction, DT as feature selection, and MLP for classification. Our experimental results illustrate that the proposed method improves the performance on the gene expression microarray data in the accuracy. Further study of our experiment indicates that not all the top eigenvectors of PCA are useful for classification, the tail eigenvector also contain discriminative information. Therefore, it is necessary to combine feature selection with feature extraction for dimension reduction for analyzing high dimensional problems.

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